

**TO'RTBURCHAKAKLI IKKI QARAMA-QARSHI TOMONI ERKIN  
PLASTINKANING ERKIN TEBRANISHINI TEKSHIRISH**

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### **Annotatsiya**

Ushbu ishda elastik plastinkaning chiziqli tebranishlari masalasi qaralgan. Plastinka materiali gisteresis tipidagi elastik dissipativlik xossasiga ega bo'lib. Qaralayotgan sistemaning matematik modeli olingan holda bir nechta holda plastinkaning tebranishlari qarab o'tilgan.

**Kalit so'zlar:** Plastinka tenglamasi, burulish funksiyasi, plastinkasining antisimmetirya o'qi, juft funksiyalar saqlanishi, plastinka erkin tebranish.

Plastinka tenglamasi quyigagi ko'rinishda berilgan bo'lsa, quyida bir nechta holini qarab o'tamiz.

$$D\nabla^4 w + \rho \frac{\partial^2 w}{\partial t^2} = 0, \quad (1)$$

Aniqlik uchun quyida y o'qiga parallel bo'lgan chetlari uchun klassik chegara shartlaritakrorlanadi (masalan chegaralari  $x=0$  yoki  $x=a$ ). Qistirilgan chekkasi uchun.

$$w = \frac{\partial w}{\partial x} = 0, \quad (2)$$

oddiy qo'yilgan cheti uchun ,

$$w = \frac{\partial^2 w}{\partial x^2} + v \frac{\partial^2 w}{\partial y^2} = 0 \quad (3)$$

va bo'sh cheti uchun

$$\frac{\partial^2 w}{\partial x^2} + v \frac{\partial^2 w}{\partial y^2} = \frac{\partial^3 w}{\partial x^3} + (2 - v) \frac{\partial^3 w}{\partial x \partial y^2} = 0. \quad (4)$$

$y=0$  va  $y=a$  qirralarining mos keladigan chegaraviy shartlar (2) , (3) va (4) tenglamalarda  $x$  va  $y$  ni o'zaro almashtirishdan olinadi. Ikki bo'sh qirralarining olinishidan hosil bo'lgan erkin burchak uchun burchakda qo'shimcha shart

$$\frac{\partial^2 w}{\partial x \partial y} = 0 \quad (5)$$

bajarilishi kerak, garchi ikkita qarama-qarshi tomoni erkin bo'lsa, bu hol yuzga kelmaydi, Erkin tebranish uchun sinusoidal vaqt reaksiyasi faraziga ko'ra

$$w(x, y, t) = w(x, y)e^{i\omega t}, \quad (6)$$

klassik Voiyt yechimi

$$w_m = [A_m \sin \sqrt{k^2 - \alpha^2} y + B_m \cos \sqrt{k^2 - \alpha^2} y + C_m \sinh \sqrt{k^2 + \alpha^2} y + D_m \cosh \sqrt{k^2 + \alpha^2} y] \sin \alpha x \quad (7)$$

olinadi, bu yerda  $k^4 = \rho\omega^2/D$ , va  $\alpha = m\pi/a$ ,  $m=1,2,\dots$ , va bu yerda  $k^2$  dan katta deb qabul qilingan. Burulish funktsiyasi (6) boshqaruv maydon tenglamasini (1) va oddiygina qo'llab quvatlanadigan chegaraviy shartlarni almashtirish har bir m uchun to'rtinchchi tartibli xarakterli determinantga olib keladi. Determinantni kengaytirish va hadlarni yig'ish xarakterli tenglamani beradi. Olti holat uchun xarakteristik tenglamalar quyida keltirilgan.

1-hol. SS-SS-SS-SS

$$\sin \varphi_1 \sinh \varphi_2 = 0 \quad (8)$$

2-hol. SS-C-SS-C

$$\varphi_1 \varphi_2 (\cos \varphi_1 \cosh \varphi_2 - 1) - m^2 \pi^2 \left(\frac{b}{a}\right)^2 \sin \varphi_1 \sinh \varphi_2 = 0. \quad (9)$$

3-hol. SS-C-SS-SS

$$\varphi_1 \tanh \varphi_2 - \varphi_2 \tan \varphi_1 = 0. \quad (10)$$

4-hol. SS--SS-F

$$\varphi_1 \varphi_2 [\gamma^2 - m^4 \pi^4 (1-v)^2] + \varphi_1 \varphi_2 [\gamma^2 + m^4 \pi^4 (1-v)^2] \cos \varphi_1 \cosh \varphi_2 + m^2 \pi^2 \left(\frac{b}{a}\right)^2 [\gamma^2 (1-2v) - m^4 \pi^4 (1-v)^2] \sin \varphi_1 \sinh \varphi_2 = 0. \quad (11)$$

5-hol. SS-SS-SS-F

$$\varphi_1 [\gamma + m^2 \pi^2 (1-v)]^2 \tanh \varphi_2 - \varphi_2 [\gamma + m^2 \pi^2 (1-v)]^2 \tan \varphi_1 = 0. \quad (12)$$

6-hol. SS-F-SS=F

$$2\varphi_1 \varphi_2 [\gamma^2 - m^4 \pi^4 (1-v)^2]^2 (\cos \varphi_1 \cosh \varphi_2 - 1) + \{\varphi_1^2 [\gamma + m^2 \pi^2 (1-v)]^2 - \varphi_2^2 [\gamma - m^2 \pi^2 (1-v)]^4\} \sin \varphi_1 \sinh \varphi_2 = 0 \quad (13)$$

(8) dan (13) tenglamalarda  $\gamma$  parameter bilan aniqlanadi

$$\gamma = \omega a^2 \sqrt{\rho/D} \quad (14)$$

va  $\varphi_1$  va  $\varphi_2$  berilgan funksiyalardir

$$\begin{aligned} \varphi_1 &= \frac{b}{a} \sqrt{\gamma - m^2 \pi^2}. \\ \varphi_2 &= \frac{b}{a} \sqrt{\gamma + m^2 \pi^2}. \end{aligned} \quad (15)$$

Adabiyotda tez-tez e'tibordan chetda qoladigan nuqta shundaki  $k^2$  kichik bo'lishi mumkin (ya'ni  $m^2 \pi^2$  dan kichik) Bu sodir bo'lganda (7) tenglamadagi  $\sin \sqrt{k^2 - \alpha^2} y$  va  $\cos \sqrt{k^2 - \alpha^2} y$  ni mos ravishda  $\sinh \sqrt{k^2 - \alpha^2} y$

va  $\cosh \sqrt{k^2 - \alpha^2} y$  bilan almashtirish kerak bo‘ladi. Keyin xarakteristik tenglamalar quydagicha bo‘ladi.

1-hol. SS-SS-SS-SS

$$\sin \beta_1 \sinh \beta_2 = 0 \quad (16)$$

2-hol. SS-C-SS-C

$$\beta_1 \beta_2 (\cos \beta_1 \cosh \beta_2 - 1) - m^2 \pi^2 \left(\frac{b}{a}\right)^2 \sin \beta_1 \sinh \beta_2 = 0. \quad (17)$$

3-hol. SS-C-SS-SS

$$\beta_1 \tanh \beta_2 - \beta_2 \tan \beta_1 = 0. \quad (18)$$

4-hol. SS--SS-F

$$\beta_1 \beta_2 [\gamma^2 - m^4 \pi^4 (1-v)^2] + \beta_1 \beta_2 [\gamma^2 + m^4 \pi^4 (1-v)^2] \cos \beta_1 \cosh \beta_2 + m^2 \pi^2 \left(\frac{b}{a}\right)^2 [\gamma^2 (1-2v) - m^4 \pi^4 (1-v)^2] \sin \beta_1 \sinh \beta_2 = 0. \quad (19)$$

5-hol. SS-SS-SS-F

$$\beta_1 [\gamma + m^2 \pi^2 (1-v)]^2 \tanh \beta_2 - \beta_2 [\gamma + m^2 \pi^2 (1-v)]^2 \tan \beta_1 = 0. \quad (20)$$

6-hol. SS-F-SS=F

$$2\beta_1 \beta_2 [\gamma^2 - m^4 \pi^4 (1-v)^2]^2 (\cos \beta_1 \cosh \beta_2 - 1) + \{\beta_1^2 [\gamma + m^2 \pi^2 (1-v)]^2 - \beta_2^2 [\gamma - m^2 \pi^2 (1-v)]^4\} \sin \beta_1 \sinh \beta_2 = 0 \quad (21)$$

(16)-(21) tenglamalar (8)-(13) tenglamalar bilan bir xil shakilda bo‘ladi, birinchisi ikkinchisida sin, cos va tanni oddiygina sinh, cosh va tanh bilan almashtirish orqali olingan  $\varphi_1 \varphi_2$  va  $\beta_1 \beta_2$  almashtirishlardir.

$$\beta_1 = \frac{b}{a} \sqrt{m^2 \pi^2 - \gamma}$$

$$\beta_2 = \frac{b}{a} \sqrt{m^2 \pi^2 + \gamma} \quad (22)$$

1, 2, va 6 holatlardagi  $y=b/2$  o‘qiga nisbatdan mavjud bo‘lgan simmetriya (ya’ni ‘y-simmetiya’) tufayli, bu holatdagi tebranishlar rejimlari y bo‘lganlarga bo‘linadi y-simmetrik yoki y-antisimmetrik. Bu rejimga mos keladigan xarakteristik tenglamalar (8), (9), (13), (16), (17) va (21) tenglamalardan faktor yo‘li bilan yoki y koordinatasi bo‘yicha yangi hosilalar yordamida olish mumkin. Sistema kelib chiqishi plastinka o‘rtasida ( $y=y-b/2$  va, masalan  $k^2 > \alpha^2$  ( $\gamma^2 > m^2 \pi^2$ ) ga ega bo‘lgan Sistema uchun (7) tenglamada y ning faqat juft funksiyalarini saqlab qolgan hol) olingan xarekteristik tenglamalar quydagilardir

1-hol. SS-SS-SS-SS

$$\text{simmetrik: } \cos \frac{\varphi_1}{2} \cosh \frac{\varphi_2}{2} \quad (23a)$$

$$\gamma^2 > m^2 \pi^2$$

$$\text{antisimmetrik: } \sin \frac{\varphi_1}{2} \sinh \frac{\varphi_2}{2} \quad (23b)$$

simmetirik:  $\cos \frac{\beta_1}{2} \cosh \frac{\beta_2}{2} = 0$  (23c)

$\gamma^2 < m^2\pi^2$

antisimmetirik:  $\sin \frac{\beta_1}{2} \sinh \frac{\beta_2}{2} = 0$  (23d)

2-hol. SS-C-SS-C

simmetirik:  $\varphi_1 \tan \frac{\varphi_1}{2} + \varphi_2 \tanh \frac{\varphi_2}{2} = 0.$  (24a)

$\gamma^2 > m^2\pi^2$

antisimmetirik:  $\varphi_1 \tan \frac{\varphi_1}{2} - \varphi_2 \tanh \frac{\varphi_2}{2} = 0.$  (24b)

simmetirik:  $\beta_1 \tan \frac{\beta_1}{2} + \beta_2 \tanh \frac{\beta_2}{2} = 0.$  (24c)

$\gamma^2 < m^2\pi^2$

antisimmetirik:  $\beta_1 \tan \frac{\beta_1}{2} - \beta_2 \tanh \frac{\beta_2}{2} = 0.$  (24d)

6-hol.

simmetiirk:  $\varphi_1 [\gamma + m^2\pi^2(1-v)]^2 \tan \frac{\varphi_1}{2} + \varphi_2 [\gamma + m^2\pi^2(1-v)]^2 \tanh \frac{\varphi_1}{2} = 0.$  (25a)

tisimmetirk:  $\varphi_1 [\gamma + m^2\pi^2(1-v)]^2 \tan \frac{\varphi_1}{2} - \varphi_2 [\gamma + m^2\pi^2(1-v)]^2 \tanh \frac{\varphi_1}{2} = 0.$  (25b)

simmetiirk:  $\beta_1 [\gamma + m^2\pi^2(1-v)]^2 \tan \frac{\beta_1}{2} + \beta_2 [\gamma + m^2\pi^2(1-v)]^2 \tanh \frac{\beta_1}{2} = 0.$  (25c)

tisimmetirk:  $\beta_1 [\gamma + m^2\pi^2(1-v)]^2 \tan \frac{\beta_1}{2} - \beta_2 [\gamma + m^2\pi^2(1-v)]^2 \tanh \frac{\beta_1}{2} = 0.$  (25d)

bundan tahqari (24b) va (24d) tenglamalar bilan bir xil ekanligi ko‘rinib turibdi , bunan tashqari  $\varphi_1$  va  $\varphi_2$  lar ,  $\frac{\varphi_1}{2}$  va  $\frac{\varphi_2}{2}$  bilan almashtirildi. Buning ahamiyati shundaki , SS-C-SS-C kengligi b bo‘lgan SS-C-SS-SS plastinkaning y-antisimmetirik tebranish rejimlari SS-C-SS-SS plastinkaniki bilan bir xil. Kengligi b/2 . buning sababi SS=C-SS-C plastinkasining antisimmetirya o‘qi bo‘ylab shartlar oddiy tayanch shartlari bilan bir xil. SS-F-SS-F plastinka va tenglamalar (12) va (20) uchun.



## **Adabiyotlar**

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